

MULTILEVEL ANALYSIS IN THE STUDY OF CRIME AND JUSTICE

“The most pervasive fallacy of philosophic thinking goes back to neglect of context”

(John Dewey, 1931)

Neither criminal behavior nor society’s reaction to it occurs in a social vacuum – for this reason criminology as a discipline is inherently a multilevel enterprise. Individual criminal behavior is influenced by larger social, political and environmental factors, as are the decisions of various actors in the criminal justice system. Classroom and school characteristics affect adolescent development, misconduct and delinquency (Beaver et al. 2008; Osgood and Anderson, 2004; Stewart, 2003). Family and neighborhood characteristics influence the likelihood of victimization and offending as well as post-release recidivism and fear of crime (Nieuwbeerta et al., 2008; Wilcox et al., 2007; Lauritsen and Schaum, 2004; Kubrin and Stewart, 2006; Wyant, 2008; Lee and Ulmer, 2000). Police department, precinct and neighborhood factors affect police arrest practices, use of force and clearance rates (Smith, 1986; Sun et al. 2008; Lawton, 2007; Pare et al. 2007; Eitle et al. 2005; Terrill and Reisig, 2003). Judge characteristics and court contexts affect individual punishment decisions (Britt, 2000; Ulmer and Johnson, 2004; Johnson, 2006; Wooldredge, 2007) and prison environments are tied to inmate misconduct, substance use and violence (Camp et al. 2003; Gillespie 2005; Huebner, 2003; Wooldredge et al. 2001). Although these examples cover a diverse array of criminological topics, they all share a common analytical quality – each involves data that are measured across multiple units of analysis. When this is the case, multilevel models offer a useful statistical approach for studying diverse issues in crime and justice. As Table 1 demonstrates, recent years have witnessed an abundance of multilevel studies across a variety of topics in criminology and criminal justice.

This chapter provides a basic introduction to the use of multilevel statistical models in the field. It begins with a conceptual overview explaining what multilevel models are and why they are necessary. It then provides a statistical overview of basic multilevel models, illustrating their application using punishment data from federal district courts. The chapter concludes with a discussion of advanced applications and common concerns that arise in the context of multilevel research endeavors.

CONCEPTUAL OVERVIEW

Multilevel statistical models are necessitated by the fact that social relationships exist at several different levels of analysis that jointly influence outcomes of interest. Smaller units of analysis are often “nested” within one or more larger units of analysis. For instance, students are nested within classrooms and schools, offenders and victims are both nested within family and neighborhood environments, and criminal justice personnel are nested within larger community and organizational contexts. In each of these cases, the characteristics of some larger context are expected to influence individual behavior. This logic can be extended to any situation involving multiple levels of analysis including but not limited to individuals, groups, social networks, neighborhoods, communities, counties, states and even countries. Moreover, longitudinal research questions often involve multilevel data structures, with repeated measures nested within individuals or with observations nested over time (e.g. Horney et al. 1995; Slocum et al. 2005; Rosenfeld et al. 2007). Other common applications of multilevel analysis include twin studies with paired or clustered sibling dyads (e.g. Wright et al. 2008; Taylor et al. 2002) and meta-analyses that involve multiple effect sizes nested within the same study or dataset (e.g. Raudenbush, 1984; Goldstein et al. 2000). Regardless of the level of aggregation or “nesting,” though, the important point is that criminological enterprises often involve data that span multiple levels of analysis. In fact, given the complexity of our social world, it can be difficult to identify topics of criminological interest that are not characterized by multiple spheres of social influence. When these multiple influences are present, multilevel statistical models represent a useful and even necessary tool for analyzing a broad variety of criminological research questions.

A MODEL BY ANY OTHER NAME?

Given the complexity surrounding multilevel models, it is useful to distinguish up front what can sometimes be a confusing and inexact argot. Various monikers are used to describe multilevel statistical models (e.g. multilevel models, hierarchical models, nested models, mixed models). Although this nomenclature is often applied interchangeably, there can be subtle but important differences in these designations. Multilevel modeling is used here as a broad, all-encompassing rubric for statistical models

that are explicitly designed to analyze and infer relationships for more than one level of analysis.¹ The language of multilevel models is further complicated by the fact that there are various different software packages that can be used to estimate multilevel models, some of which are general statistical packages (e.g. SAS, STATA) and others that are specialized multilevel programs (e.g. HLM, MLwin, aML).²

Additional confusion may derive from the fact that scholars often use terminology such as ecological, aggregate and contextual effects interchangeably despite important differences in their meaning. *Ecological effects*, or group-level effects, can refer to any group level influence that is associated with the higher level of analysis. Group level effects can take several forms. First, *aggregate effects* (sometimes referred to as *analytical* or *derived* variables) are created by aggregating individual level characteristics up to the group level of analysis (e.g. percent male in a school). These are sometimes distinguished from *structural effects* that are also derived from individual data but capture relational measures among members within a group (e.g. density of friendship networks) (see Luke, 2004: 6). To complicate matters, when individual level data are aggregated to the group level they can exert two distinct types of influence – first, they can exert *compositional effects* which reflect group differences that are attributable to variability in the constitution of the groups – between-group differences may simply reflect the fact that groups are made up of different types of individuals. Second they can exert *contextual effects* which represent influences above and beyond differences that exist in group composition. Contextual effects are sometimes referred to as *emergent properties* because the collective exerts a synergistic influence that is unique to the group aggregation and which is not present in the individual

¹ Hierarchical or nested models, for instance, technically refer to data structures involving exact nesting of smaller levels of analysis within larger units. Multilevel data, however, can also be non-nested, or “cross-classified”, in ways that do not follow a neat hierarchical ordering. Data might be nested within years and within states at the same time, for example, with no clear hierarchy to “year” and “state” as levels of analysis (Gelman and Hill, 2007: 2). Similarly, adolescents might be nested within schools and neighborhoods with students from the same neighborhood attending different schools. Although these cases clearly involve multilevel data, they are not hierarchical in a technical sense. Similarly, “mixed models” technically refer to statistical models containing both “fixed” and “random” effects. Although this often is the case in multilevel models, it is not necessarily the case, so the broader rubric multilevel modeling is preferred to capture the variety of models designed to incorporate data across multiple units of analysis.

² A useful and detailed review of the strengths and limitations of numerous software programs that provide for the estimation of multilevel models is provided by the Centre for Multilevel Modeling at the University of Bristol at <http://www.cmm.bris.ac.uk/learning-training/multilevel-m-software/index.shtml>.

constituent parts.³ Although the term “contextual effect” is sometimes used as a broader rubric for any group level influence, the narrower definition provided here is often useful for distinguishing among types of ecological influences that can be examined in multilevel models. Finally, *global effects* refer to structural characteristics of the collective itself that are not derived from individual data but rather reflect measures that are specific to the group (e.g. physical dilapidation of the school). These and other commonly used terms in multilevel analysis are summarized in Table 2.⁴

THEORETICAL RATIONALES FOR MULTILEVEL MODELS

The need for multilevel statistical models is firmly rooted in both theoretical and methodological rationales. Multilevel models are extensions of traditional regression models that account for the structuring of data across aggregate groupings, that is, they explicitly account for the nested nature of data across multiple levels of analysis. Because our social world is inherently multilevel, theoretical perspectives that incorporate multiple levels of influence in the study of crime and justice are bound to improve our ability to explain both individual criminal behavior and society’s reaction to it.

Figure 1 presents a schematic of a hypothetical study examining the influence of low self-control on delinquency in a sample of high school students. Imagine that self-control is measured at multiple time points for the same sample of students. In that case, multiple measures of self-control would be nested within individual students, and individual students would be nested within classrooms which are nested within schools. The lowest level of analysis would be within-individual observations of self-control, and the highest level of analysis would be school-level characteristics. Ignoring this hierarchical data structuring, then, is likely to introduce omitted variable bias of a large-scale theoretical nature.

³ Philosophical discourse on emergent properties dates all the way back to Aristotle but was perhaps most lucidly applied by John Stuart Mill. He argued that the human body in its entirety produces something uniquely greater than its singular organic parts, stating that “To whatever degree we might imagine our knowledge of the properties of the several ingredients of a living body to be extended and perfected, it is certain that no mere summing up of the separate actions of those elements will ever amount to the action of the living body itself” (Mill, 1843). Contextual effects models have long been applied in sociology and related fields (e.g. Firebaugh, 1978; Blalock, 1984), but these applications differ from multilevel models in that the latter are more general formulations that specifically account for residual correlation within groups and explicitly provide for examination of the causes of between-group variation in outcomes.

⁴ Table 2 is partially adapted from Diez Roux (2002) which contains a more detailed and elaborate glossary of many of these terms.

Moreover, many theoretical perspectives explicitly argue that micro-level influences will vary across macro-social contexts. For instance, racial group threat theories (Blumer, 1958; Liska, 1992) predict that the exercise of formal social control will vary in concert with large or growing minority populations. Testing theoretical models that explicitly incorporate variation in micro-effects across macro-theoretical contexts therefore offers an important opportunity to advance criminological knowledge. Assuming that theoretical influences operate at a single level of analysis is likely to provide a simplistic and incomplete portrayal of the complex criminological social world.

Moreover, inferential problems can emerge when data are used to draw statistical conclusions across levels of analysis. For instance, in his classic study of immigrant literacy, Robinson (1950) examined the correlation between aggregate literacy rates and the proportion of the population that was immigrant at the state level. He found a substantial positive correlation between percent immigrant and the literacy rate ($r=.53$). Yet when individual level data on immigration and literacy were separately examined, the correlation reversed and became negative ($r=-.11$). Although individual immigrants had lower literacy, they tended to settle in states with high native literacy rates thus confounding the individual and aggregate relationships. This offers an example of the *ecological fallacy*, or erroneous conclusions involving individual relationships that are inferred from aggregate data. As Peter Blau (1960: 179) suggested, aggregate studies are limited because they cannot “separate the consequences of social conditions from those of the individual's own characteristics for his behavior, because ecological data do not furnish information about individuals except in the aggregate.”

The same mistake in statistical inference can occur in the opposite direction. The *atomistic (or individualistic) fallacy* occurs when aggregate relationships are mistakenly inferred from individual level data. Because associations between two variables at the individual level may differ from associations for analogous variables at a higher level of aggregation, aggregate relationships cannot be reliably inferred from individual level data. For instance, social disorganization theory would predict that crimes rates across neighborhoods are related to mobility rates because high population turnover reduces informal social control at the neighborhood level. Because this prediction refers to neighborhoods as the unit of

analysis, though, one would risk serious inferential error testing this group-level hypothesis with individual level data. For instance, one could not test the theory by examining whether or not individuals who move residences have higher criminal involvement. To do so would be to commit the atomistic fallacy. This reflects the fact that variables aggregated up from individual level data often have unique and independent *contextual* effects. Moving to a new residence represents a different causal pathway than living in a neighborhood with high rates of residential mobility.⁵

Because of the inherent difficulties in making statistical inferences across different levels of analysis, a preferred approach is to use multilevel analytic procedures to simultaneously incorporate individual and group level causal processes. Multilevel models explicitly provide for this type of statistical analysis. The difficulty is in distinguishing among the different types of individual and ecological influences that are of theoretical interest and then specifying the statistical model to properly estimate these effects.

MULTILEVEL MODELING AND HYPOTHESIS TESTING

There are also persuasive statistical reasons for engaging in multilevel modeling, such as providing improved parameter estimates, corrected standard errors, and conducting more accurate statistical significance tests. Utilizing traditional regression models for multilevel data presents several problems. Figure 2 presents a second example of hierarchical data where individual criminal offenders are nested within judges and county courts. Because several offenders are sentenced by the same judge and several judges share the same courtroom environment, statistical dependencies are likely to arise among clustered observations. When individual data is nested within aggregate groups, observations within clusters are likely to share unaccounted-for similarities. If, for instance, some judges are “hanging judges” while others are “bleeding-heart liberals,” then offenders sentenced by the former will have sentences that are systematically harsher than offenders sentenced by the latter. Statistically speaking, the

⁵ Two related but distinct problems of causal inference are the *psychologistic fallacy*, which can occur when individual level data are used to draw inferences without accounting for confounding ecological influences, and the *sociologistic fallacy* which may arise from the failure to consider individual level characteristics when drawing inferences about the causes of group variability. The psychologistic fallacy results from a failure to adequately consider *contextual effects*, whereas the sociologistic fallacy results from a failure to capture *compositional effects*.

residual errors will be correlated, systematically falling above the regression line for the first judge and below it for the second. Because one of the assumptions of ordinary regression models is that residual errors are independent, such systematic clustering would violate this core model assumption. The consequence of this violation is that standard errors will be *underestimated* by the ordinary regression model. Statistical significance tests will therefore be too liberal, risking Type I inferential errors in which the null hypothesis is falsely rejected even when true in the population. Multilevel statistical models are needed to account for statistical dependencies that occur among clusters of hierarchically organized data.⁶

A related problem is that statistical significance tests in ordinary regression models utilize the wrong degrees of freedom for ecological predictors in the model. Traditional regression models fail to account for the fact that hierarchically structured data are characterized by different sample sizes at each level of analysis. For example, with data on 1,000 students nested within 50 schools, there would be an individual level sample size of 1,000 observations but a school level sample size of only 50 observations. This means that statistical significance tests for school-level predictors need to be based on degrees of freedom that reflect the number of schools in the data, not the number of students. Statistical significance tests in ordinary regression models fail to recognize this important distinction. The consequence is that the amount of statistical power available for testing school-level predictors will be exaggerated. The number of degrees of freedom for statistical significance tests needs to be adjusted for the number of aggregate units in the data – multilevel models provide these adjustments.

A third advantage of multilevel models over ordinary regression models is that they allow for the modeling of heterogeneity in regression effects. The single-level regression model assumes *de facto* that individual predictors exert the same effect in each aggregate grouping. Multilevel models, on the other hand, explicitly allow for variation in the effects of individual predictors across higher levels of analysis.

⁶ A simpler alternative to the full multilevel model is to estimate an ordinary regression using robust standard errors that are adjusted for the clustering of observations across level 2 units. For example, STATA provides a “cluster” command option that adjusts standard errors for residual dependency. This can be a useful approach when the goal is simply to “control” for clustering, but beyond that it does not provide the same advantages of the multilevel model. Another option is to control for group-level variation using a “fixed effects” model that includes dummy variables for each level 2 unit in the data. This is a useful approach for removing the intraclass correlation due to group dependency, but it precludes examination of between-group differences.

Ulmer and Bradley, (2006), for instance, have argued that the effect of trial conviction on criminal sentence varies across courts. This proposition is illustrated in Figure 3 using federal punishment data for a random sample of 8 districts courts. The ordinary regression model would constrain the effect of trial conviction to be uniform across courts, but Figure 3 clearly suggests variation in this effect across courts. Multilevel analysis allows for this type of variation to be explicitly incorporated into the statistical model, providing the researcher with a useful tool for better capturing the real-world complexity that is likely to characterize individual influences across criminological contexts.

Other advantages that also characterize multilevel models are that they provide for convenient and accurate tests of cross-level interactions, or moderating effects that involve both individual and ecological variables. For example, the influence of individual socioeconomic status on delinquency might depend on the socioeconomic composition of the school. This conditional relationship could be directly investigated by specifying a cross-level interaction between an individual's SES and the mean SES at the school level.

One final statistical advantage of multilevel models is that they are able to simultaneously incorporate information both within and between groups in order to provide optimally-weighted group level estimates. This is accomplished by combining information from the group itself with information from other similar groups in the data, and it is particularly useful when some groups have relatively few observations. Because groups with smaller sample sizes will have less reliable group means, some regression to the overall grand mean is expected. Utilizing a Bayesian estimation approach, the multilevel model shifts the within group mean toward the mean for other groups. The more reliable the group mean, the more heavily it is weighted; the less reliable (and the less variability across groups), the more the estimate is shifted toward the overall grand mean for all groups in the data. Thus estimates for specific groups are based not only on their own within-group data, but also on data from other groups. This process is sometimes referred to as "borrowing power" because within-group estimates benefit from information on other groups, and the estimates themselves are sometimes called "shrinkage estimates" because they "shrink" individual group means toward the grand mean for all groups. The end result is

that group level estimates are optimally weighted to reflect information both within and between groups in the data.⁷

Multilevel models, then, provide numerous analytical and statistical advantages over ordinary regression approaches when data are nested across levels of analysis. By providing for the simultaneous inclusion of individual and group level information, they better specify the complex relationships that often characterize our social world, and they help overcome common problems of statistical inference associated with reliance on single-level data. Moreover, multilevel models correct for the problematic clustering of observations that may occur with nested data, they provide a convenient approach for modeling both within and between group variability in regression effects, and they offer improved parameter estimates that simultaneously incorporate within and between group information. The remaining discussion provides a basic statistical introduction to the multilevel model along with examples illustrating its application to the study of criminal punishment in federal court.

STATISTICAL OVERVIEW

Multilevel models are simple extensions of ordinary regression models, which account for the nesting of data within higher-order units. It is therefore useful to begin with an overview of the basic regression model in order to demonstrate how the multilevel adaptation builds upon and extends it to the case of multilevel data. For illustrative purposes, examples are provided using United States Sentencing Commission (USSC) data on a random sample of 25,000 convicted federal offenders nested within 89 federal district courts across the U.S.⁸

FROM ORDINARY REGRESSION TO MULTILEVEL ANALYSIS

⁷ The following equation provides the formula for this weighting process (Raudenbush and Bryk, 2002: 46):

$$\hat{\beta}_j^* = \lambda_j \bar{Y}_{\bullet j} + (1 - \lambda_j) \hat{\gamma}_{00}$$

where $\hat{\beta}_j^*$ is the group estimate, which is a product of the individual group mean $\bar{Y}_{\bullet j}$ weighted by its reliability λ_j , plus the overall grand mean $\hat{\gamma}_{00}$ weighted by the complement of the reliability $(1 - \lambda_j)$. If the reliability of the group mean is one, the weighted estimate reduces to the group mean; if it is zero, it reduces to the grand mean. The more reliable the group mean, then, the more it counts in the multilevel estimate. When the assumptions of the multilevel model are met, this provides the most precise and most efficient estimator of the group mean.

⁸ These data are drawn from fiscal years 1997 to 2000 and are restricted to the 89 federal districts and 11 circuit courts within the U.S., with the District of Columbia excluded because it has its own district and circuit court. For more information on the USSC data see Johnson et al. (2008).

When faced with multilevel data (e.g. lower-level data that is nested within some higher-level grouping), ordinary regression approaches can take three basic forms. First, individual data can be pooled across groups and analyzed without regard for group structure. This approach ignores important group-level variability and often violates key assumptions of OLS regression such as independent errors. Second, separate un-pooled analyses can be conducted within each group. This approach can be useful for examining between-group variability, but it requires relatively large samples for each group and it is cumbersome when the number of groups becomes large. Third, aggregate analysis can also be conducted at the group level alone, but this approach ignores within-group variability and requires a relatively large number of groups for analysis. In each of these cases, traditional regression approaches are unable to incorporate the full range of information available at both the individual and group level of analysis and they may violate important assumptions of the single-level ordinary regression model.

For illustrative purposes, the ordinary regression model is presented in Equation 1:

$$Y_i = \beta_0 + \beta_1 X_i + r_i \quad (1)$$

where Y_i is a continuous dependent variable, β_0 is the model intercept, β_1 is the effect of the independent variable X_i for individual i and r_i is the individual level residual error term. Two key assumptions of the linear regression model are that the relationship between X_i and Y_i can be summarized with a single linear regression line and that all of the residual error terms for individuals in the data are statistically independent of one another. Both of these assumptions are likely to be violated with multilevel data, the first because the effect of X_i on Y_i might vary by group and the second because individuals within the same group are likely to share unaccounted-for similarities.

Failure to account for the nesting of observations can result in “false power” at both levels of analysis. False power occurs because there is typically less independent information available when observations are clustered together. Consider the difference between a) data from 50 schools with 20 students each, versus b) data from 1,000 schools with one student each. The number of students is the same, but if students share similarities within schools, each student provides less unique information in the first sample than in the second. Moreover, there is more unique school level data in the second

sample than in the first. Because ordinary regression models ignore the clustering of individuals within schools, they treat both samples as equivalent. The consequence of this is that the amount of statistical power for the first sample is artificially inflated at both the individual and school level of analysis. Moreover, standard errors for the first sample will be underestimated and significance tests will be too liberal if there are unaccounted-for similarities among students within schools.

The multilevel solution is to add an additional error parameter to the ordinary regression model in order to capture group level dependencies in the data. The multilevel model is represented by a series of “submodels” that model between-group variation in individual level parameters as a function of group level processes. A basic two-level random intercept model is presented in Equation 2:

$$\begin{array}{ll} \text{Level 1} & Y_{ij} = \beta_{0j} + \beta_{1j}X_{ij} + r_{ij} \\ \text{Level 2} & \beta_{0j} = \gamma_{00} + u_{0j} \end{array} \quad (2)$$

where the level one intercept β_{0j} is modeled as an outcome in the level 2 portion of the model. The γ_{00} parameter represents the Level 2 intercept (gammas are substituted for betas at Level 2 for notational convenience) and the u_{0j} parameter represents the new group level error term, which accounts for group-level dependence. The two-level model specification is presented for simple notational convenience and can be combined into an equivalent single level model by substituting the Level 2 model in for β_{0j} at Level 1. Doing so produces the combined model in Equation 3:

$$Y_{ij} = \gamma_{00} + \beta_{1j}X_{ij} + r_{ij} + u_{0j} \quad (3)$$

Comparing Equation 3 to Equation 1, it becomes clear that the only difference between the ordinary regression model and the multilevel model is the additional group level error term u_{0j} . The basic multilevel model, then, is nothing more than an ordinary regression equation that includes an additional group-level error parameter to capture group level dependencies.

The addition of the group-level error term explicitly models variation among group means in the data. For example, if the outcome is the mean sentence length given to offenders across federal district courts, the group-level error term allows for mean sentence length to vary by federal district, thus capturing potentially important district-level differences in average punishment severity. These

differences are illustrated in Figure 4, where Panel A shows the mean sentence length pooled across a sample of ten federal districts, and Panel B shows the mean sentence length disaggregated by federal district. The figure indicates that average punishments vary across federal courts. For instance, the mean sentence length in the Northern District of Florida is about twice the average sentence in the District of Delaware. Important differences in variability in punishment also exist across federal districts, with the standard deviation in the Western District of Oklahoma being more than twice that in the Southern District of California. These group level variations are captured by the incorporation of the group-level error term in the multilevel statistical model, resulting in standard errors and statistical significance tests that are properly adjusted for the nesting of individual cases within aggregate district court groupings.

BUILDING THE MULTILEVEL MODEL

Despite its conceptual simplicity, multilevel analysis adds a layer of analytical complexity that can quickly become cumbersome when applied to research questions involving multiple predictors across multiple levels of analysis. For this reason it is essential to build the multilevel model carefully from the ground up. There are several types of multilevel models that vary in complexity, including 1) unconditional models, 2) random intercept models, 3) random coefficient models and 4) cross-level interaction models – each adds an additional layer of complexity and provides additional information in the multilevel analysis.

THE UNCONDITIONAL MODEL

The first step in multilevel analysis is to investigate the necessity of using a multilevel model. This is both a theoretical and statistical question. First, the research question should always dictate the methodology. Some research questions that involve multiple levels of data may be answerable with simpler and more parsimonious analytical approaches. So called “fixed effects” models, for instance, can be a simple and effective way of removing between-group variation. Including a series of dummy variables for level 2 units parcels out the level 2 variation and corrects for any intraclass correlation among nested observations. Before adopting a multilevel model, then, it is important to first make sure the research question necessitates multilevel analysis. Despite its advantages the multilevel model is not

always necessary, nor ideal. For instance, a minimum number of aggregate groupings is generally needed for multilevel analysis because a sufficient number of level 2 units is required for higher order statistical significance tests.⁹ It is also useful to begin by testing for the presence of correlated errors before turning to multilevel analysis. This can be done by estimating an ordinary regression, saving the residuals, and then conducting an analysis of variance to investigate whether or not the residuals are significantly related to group membership. Significant results provide evidence that the ordinary regression assumption of independent errors is violated by the nested structure of the data.

The necessity of multilevel analysis can be further investigated through the *unconditional or null model*. This model is referred to as “unconditional” because it includes no predictors at any level of analysis, so it provides a predicted value for the mean which is not conditional on any covariates. It is summarized in Equation 4:

$$\begin{array}{ll}
 \text{Level 1} & Y_{ij} = \beta_{0j} + r_{ij} \\
 \text{Level 2} & \beta_{0j} = \gamma_{00} + u_{0j}
 \end{array} \tag{4}$$

where Y_{ij} is a continuous outcome for individual i in group j , estimated by the overall intercept β_{0j} plus an individual-level error term, r_{ij} . At level 2 of the model, the intercept β_{0j} is modeled as a product of a level 2 intercept γ_{00} plus a group-level error term, u_{0j} . The unconditional model decomposes the total variance in the outcome into two parts – an individual variance, captured by the individual-level error term, and a group variance, captured by the group-level error term. The unconditional model is therefore useful for investigating the amount of variation that exists within versus between groups. One way to

⁹ Scholars disagree on this point. Some advocate using multilevel models in any situation involving nested data (e.g. Gelman and Hill, 2007) while others caution its use in analyses involving relatively few level 2 units (e.g. Snijders and Bosker, 1999: 44). Although there does not seem to be widespread consensus on what constitutes a sufficient number of groups (in part because the number of observations per grouping also matters), a general rule of thumb might be to require about a dozen or so groupings before turning to multilevel analysis, at least for analyses that include level 2 predictors. This issue in part reflects concerns over statistical power in multilevel analysis, which is a product of several factors including the number of clusters, the number of observations per cluster, the strength of the intraclass correlation and the effect sizes for level 2 variables in the model, all of which will affect the decision to employ multilevel analysis. A useful optimal design software program for conducting power analysis with multilevel data is available at: http://sitemaker.umich.edu/group-based/optimal_design_software.

quantify this is to calculate the intraclass correlation coefficient (ICC), which represents the proportion of the total variance that is attributable to between-group differences. The ICC is represented by Equation 5:

$$\rho = \frac{\tau_{00}}{(\sigma^2 + \tau_{00})} \quad (5)$$

where τ_{00} is the between-group variance estimated by the u_{0j} parameter and σ^2 is the within-group variance estimated by the r_{ij} parameter in Equation 4. The intraclass correlation is the ratio of between group variance to total variance in the outcome. Larger ICCs indicate that a greater proportion of the total variance in the outcome is due to between-group differences.¹⁰ It is important to begin any multilevel analysis by estimating the unconditional model. It provides an assessment of whether or not significant between-group variation exists – if it does not, then multilevel analysis is unnecessary – and it serves as a useful baseline model for evaluating explained variance in subsequent model specifications.

Table 3 presents the results from an unconditional model examining sentence length for a random sample of federal offenders nested within U.S. district courts. The results are broken into two parts, one for the “fixed effects”, which report the unstandardized regression coefficients, and one for the “random effects”, which report the variance components for the model. The overall intercept is 52.5 months indicating that the average federal sentence in this sample is just under 5 years. The level 1 variance provides a measure of within-district variation in sentence lengths and the level 2 variance provides an analogous measure for between-district variation. The significance test associated with the level 2 variance component indicates there is significant between district variation in sentences – sentence lengths vary significantly across federal district courts. Notice that the significance test uses degrees of freedom for the number of level 2 rather than level 1 units; it provides preliminary evidence that districts

¹⁰ It is common in multilevel analysis for between-group variation to represent a relatively small proportion of the total variance, however, as Liska (1990) argues, this does not indicate that between group variation is unimportant.

matter in federal punishment, although as Luke (2004) points out, significance tests for variance components should always be interpreted cautiously.¹¹

In order to get a sense of the magnitude of inter-district variation in punishment, the intraclass correlation coefficient (ICC) can be calculated and the random effects can be assessed in combination with the fixed effects in Table 3. The level 2, or between group, variance is $\tau_{00} = 267$ and the within-group, or individual variance is $\sigma^2 = 4,630$. Plugging these values into Equation 5 gives an ICC equal to .055. This indicates that 5.5% of the total variation in sentence length is attributable to between-district variation in sentencing. Similarly, the standard deviation for the between group variance component can be added and subtracted to the model intercept to provide a range of values for average sentences among districts. Adding and subtracting 16 months gives a range between 36.2 and 68.9 months, so the average sentence varies between 3 years and 5 ³/₄ years for one standard deviation (i.e. about two-thirds) of federal district courts. The significance test, intraclass correlation and range of average sentences all suggest important between-group variation, indicating that multilevel analysis is appropriate in this instance.

THE RANDOM INTERCEPT MODEL

The second type of multilevel model adds predictor variables to the unconditional model and is referred to as a random intercept model because it allows the intercept to take on different values for each level 2 unit in the data. There are three types of random intercept models – models that include only level 1 predictors, models that include only level 2 predictors, and models that include both level 1 and level 2 predictors. In the first model, the focus of the multilevel analysis is on controlling for statistical dependence in clustered observations. In the second the focus is on estimating variation in group means as a function of group-level predictors, and in the third, the focus is on estimating the joint influence of both level 1 and level 2 predictors. The type of random intercept model will depend on the research

¹¹ Variances are bounded by zero so they are not normally distributed and they are usually expected to take on non-zero values anyway so it is not always clear what a significant variance means. Although significance tests for variance components can provide a useful starting point, then, they should be used judiciously. It is much more useful to interpret the substantive magnitude of the variance component rather than just its statistical significance.

question of interest, but it is often useful to begin by estimating the model with only level 1 predictors.

This model is presented in Equation 6:

$$\begin{array}{ll}
 \text{Level 1} & Y_{ij} = \beta_{0j} + \beta_{1j}X_{ij} + r_{ij} \\
 \text{Level 2} & \beta_{0j} = \gamma_{00} + u_{0j}
 \end{array} \tag{6}$$

where X_{ij} represents an individual level predictor added to the unconditional model in Equation 4. Again the level 2 equation models the level 1 intercept β_{0j} as a product of both the overall mean intercept, γ_{00} , and a unique level 2 error term, u_{0j} . Substantively this means that the model intercept is allowed to vary randomly across level 2 units; each level 2 unit in the sample has its own group-specific intercept, just as if separate regressions were estimated for each group in the data.

Table 4 presents the results from a model examining the impact of the severity of the offense on the final sentence. In this model offense severity is centered around its grand mean (see discussion of centering below) and added to the level 1 portion of the model as a predictor of sentence length. β_{1j} in Equation 6 represents the effect of offense severity, X_{ij} , on the length of one's sentence in federal court. It is interpreted just as it would be in an ordinary regression model – each one unit increase in offense severity increases one's sentence length by 5.56 months. The average sentence is also allowed to vary by federal district, however. This is reflected by the level 2 variance component u_{0j} in Table 4. Both variance components now represent residuals, or left-over variation that is unaccounted for by the model. Notice that the deviance statistic is reduced from the unconditional to the conditional model, indicating increased model fit.¹² To better quantify the model fit, it is often useful to calculate proportionate

¹² The deviance statistic is equal to -2 times the natural log of the likelihood function and serves as a measure of lack of fit between the model and the data – the smaller the deviance the better the model fit. The inclusion of additional predictors will decrease the model deviance, and although the deviance is not directly interpretable it is useful for comparing alternative model specifications to one another (Luke, 2004). The difference in deviance statistics for two models is distributed as a chi-square distribution with degrees of freedom equal to the difference in the number of parameters in the two models. Multilevel models are typically fit with maximum likelihood estimation but this can be done using either full maximum likelihood (ML) or restricted maximum likelihood (REML). Both estimators will produce identical estimates of the fixed effects, but REML will produce variance estimates that are less biased than ML when the number of level 2 units is relatively small (see Kreft and DeLeeuw, 1998: 131-133; Snidjers and Bosker, 1999: 88-90). REML is useful for testing two nested models that differ only in their random effects (e.g. an

reduction of error (PRE) measures that approximate R^2 statistics for explained variance at each level of analysis. Equation 7 provides the formulas for these calculations:

$$R_{Lev1}^2 = \frac{\sigma_{unc}^2 - \sigma_{cond}^2}{\sigma_{unc}^2} \quad (7)$$

$$R_{Lev2}^2 = \frac{\tau_{unc} - \tau_{cond}}{\tau_{unc}}$$

where explained variation at level 1 is calculated by examining the reduction in level 1 variance relative to the total variance from the unconditional model reported in Table 3. The unconditional estimate of level 1 variance was 4,639 and the conditional (i.e. controlling for offense severity) estimate is 2,228.7. This difference (2,401.3) divided by the total unconditional variance (4,630) provides an R^2 estimate of .519, so offense severity explains over 50% of the variance in sentence lengths among federal offenders.

The inclusion of level 1 predictors can also explain between-district variation at level 2 of the analysis. This is because there may be important differences in offense severity across districts, with some districts systematically facing more serious crime than others. Explained variation at level 2 is calculated by examining the reduction in level 2 variance from the unconditional to the conditional model. The unconditional estimate for between-district variation was 267.1 and the conditional estimate is 93.2. The difference (173.9) divided by the total (267.1) provides an estimate of explained variation at level 2 equal to .651. This indicates that 65% of inter-district variation in sentences is due to the fact that districts vary in the severity of the crimes they face, or 65% of district variation is attributable to *compositional* differences in offense severity.¹³

The random intercept model can be expanded to also include a level 2 predictor as in Equation 8:

additional random coefficient in the model), but ML must be used to compare models that also differ in their fixed effects (e.g. an additional predictor variable). All example models herein are estimated with REML.

¹³ These basic formulas for explained variance are simple to apply and often quite useful, but in some circumstances it is possible for the inclusion of additional predictors to result in smaller or even negative values for explained variance (Snijders and Bosker, 1999: 99-100). Slightly more complicated alternative formulas are also available that include adjustments for the average number of level 1 units per level 2 unit (see e.g. Luke, 2004: 36). Total explained variance at both levels of analysis can be computed using the combined formula:

$$R_{Total}^2 = \frac{(\sigma_{unc}^2 + \tau_{unc}) - (\sigma_{cond}^2 + \tau_{cond})}{\sigma_{unc}^2 + \tau_{unc}}$$

$$\begin{array}{ll}
\text{Level 1} & Y_{ij} = \beta_{0j} + \beta_{1j}X_{ij} + r_{ij} \\
\text{Level 2} & \beta_{0j} = \gamma_{00} + \gamma_{01}W_j + u_{0j}
\end{array} \tag{8}$$

Group mean differences in the intercept, β_{0j} , are now modeled as a product of a group-level predictor, W_j , with γ_{01} representing the effect of the level 2 covariate on the outcome of interest. Level 2 predictors can take several forms including aggregate, structural or global measures (see Table 2). Results for the model including the individual level 1 predictor (offense severity) and the level 2 predictor (Southern location) are presented in Table 5. The effect of offense severity remains essentially unchanged, but districts in the South sentence offenders to an additional 7.1 months of incarceration. Although level 1 variables can explain variation at both levels of analysis, level 2 variables can only explain between-group variation at level 2. Accordingly, the level 2 predictor South does not alter the level 1 variance estimate but it does reduce the level 2 variance from 93.2 to 82.4. This is a reduction of 11.6% so Southern location accounts for just under 12% of the residual level 2 variance after controlling for offense severity. Equation 8 includes only one level 1 and one level 2 predictor, but the model can be easily expanded to include multiple predictors at both levels of analysis. Although the random intercept model allows the group means to vary as a product of level 2 predictors, it assumes that the effects of the level 1 predictors are uniform across level 2 units. This assumption can be investigated and if it is violated then a random coefficient model may be more appropriate.

THE RANDOM COEFFICIENT MODEL

The random coefficient model builds upon the random intercept model by allowing the effects of individual predictors to also vary randomly across level 2 units. That is, the level 1 slope coefficients are allowed to take on different values in different aggregate groupings. The difference between the random intercept and random coefficient model is graphically depicted in Figure 5, where each line represents the effect of some X on Y for 3 hypothetical groupings. In the random intercept model, the slopes are constrained to be the same for all 3 groups but the intercepts are allowed to be different. In the random coefficient model, both the intercepts and slopes are allowed to differ across the 3 groups – the effect of X

on Y varies by group. Mathematically, the random coefficient model (with a single level 1 predictor) is represented by Equation 9:

$$\begin{aligned}
 \text{Level 1} \quad & Y_{ij} = \beta_{0j} + \beta_{1j}X_{ij} + r_{ij} \\
 \text{Level 2} \quad & \beta_{0j} = \gamma_{00} + u_{0j} \\
 & \beta_{1j} = \gamma_{10} + u_{1j}
 \end{aligned} \tag{9}$$

where the key difference from Equation 6 is the addition of the new random error term u_{1j} associated with the effect of X_{ij} on Y_{ij} . That is, the β_{1j} slope coefficient is modeling with a random variance component, allowing it to take on different values across level 2 units. For instance, the treatment effect of an after-school delinquency program might vary by school context, being more effective in some schools than others (Gottfredson et al. 2007). The random coefficient model can capture this type of between-group variation in the effect of the independent variable on the outcome of interest.

The decision to specify random coefficients should be based on both theory and empiricism. Regarding federal sentencing data, it might make theoretical sense to investigate variations in the effect of offense severity across courts because some literature suggests perceptions of crime seriousness involve a relative evaluation by court actors (Emerson, 1983). Definitions of “serious” crime might be different in different court contexts. To test this proposition, the deviance statistics can be compared for two models, one with offense severity specified as a fixed (i.e. non-varying) coefficient as reported in Table 4 and one with it specified as a random coefficient as in Table 6. The deviance for the random intercept model is 263,876 and the deviance for the random coefficient model is 262,530. The difference produces a chi-square statistic of 1,346 with 2 degrees of freedom which is highly significant.¹⁴ The null hypothesis can therefore be rejected in favor of the random coefficient model.

¹⁴ The difference in the number of parameters is equal to 2 because the addition of the random coefficient introduces both an additional variance component and an additional covariance component to the model: $Var \begin{bmatrix} u_{0j} \\ u_{1j} \end{bmatrix} = \begin{bmatrix} \tau_{00} & \tau_{01} \\ \tau_{10} & \tau_{11} \end{bmatrix}$

where τ_{11} is the new variance associated with the random coefficient β_{1j} . Because the models only differ in their random components, REML estimation is used for this comparison.

Additional evidence in support of the random coefficient model is provided by the highly significant p-value for the u_{ij} parameter in Table 6. This suggests there is significant variation in the effect of offense severity across district courts. To quantify this effect, the standard deviation (s.d.=1.2) for the random effect can be added and subtracted to the coefficient (b=5.7) for offense severity. This suggests that each unit increase in offense severity increases one's sentence length between 4.5 and 6.9 months for one standard deviation (i.e. about two-thirds) of federal district courts. One final diagnostic tool for properly specifying fixed and random coefficients is to compare differences between model-based and robust standard errors.¹⁵ Discrepancies between the two likely indicate model misspecification, such as level 1 coefficients that should be specified as random rather than fixed effects.

To demonstrate, Table 7 provides a comparison of an OLS, random intercept and random coefficient model, along with a pictorial representation of each. As expected, the standard errors in the OLS model are underestimated. The standard error for the model intercept, for instance, increases from .30 to 1.10 from the OLS to the random intercept model. Examining the robust standard errors in the random intercept model suggests there may be a problem – the robust standard error for offense severity is more than 6 times as large as its model-based standard error. This is consistent with earlier results that suggested significant variation exists in the effect of offense severity across districts. Allowing for this variation in the random coefficient model produces model-based and robust standard error estimates for offense severity that are identical. Large differences in robust standard errors can serve as a useful diagnostic tool for identifying misspecification in the random effects portion of the multilevel model.

These diagnostic approaches, along with theoretical considerations, should be used to gradually build the random effects portion of the random coefficient model. Ecological predictors can also be included at level 2 of the random coefficient model. Table 8 reports the results for the random coefficient

¹⁵ Robust standard errors are standard errors that are adjusted to account for possible violations of underlying model assumptions regarding error distributions and covariance structures (see Raudenbush and Bryk, 2002: 276). In the case of multilevel models, these violations can lead to misestimated standard errors that result in faulty statistical significance tests. Robust standard errors provide estimates that are relatively insensitive to model misspecifications, but because the calculation of robust standard errors relies on large sample properties, they should only be used when the number of level 2 units is relatively large.

model adding Southern location as a level 2 predictor. Notice that the estimated effect of South is less in the random coefficient model in Table 8 than it was in the random intercept model in Table 5. This highlights the importance of properly specifying the random effects portion of the multilevel model – changes in the random effects at level 1 can alter the estimates for both level 1 and level 2 predictors.

Often times the final multilevel model will include a mixture of fixed and random coefficients, which is why it is sometimes called the “mixed model.” Equation 10 provides an example of a mixed model with two level 1 predictors and 1 level 2 predictor:

$$\begin{aligned}
 \text{Level 1} \quad & Y_{ij} = \beta_{0j} + \beta_{1j}X_{1ij} + \beta_{2j}X_{2ij} + r_{ij} \\
 \text{Level 2} \quad & \beta_{0j} = \gamma_{00} + \gamma_{01}W_j + u_{0j} \\
 & \beta_{1j} = \gamma_{10} + u_{1j} \\
 & \beta_{2j} = \gamma_{20}
 \end{aligned} \tag{10}$$

In this mixed model, the effect of the first independent variable X_{1ij} is allowed to have varying effects across level 2 units because its coefficient β_{1j} in level 2 of the model includes the random error term u_{1j} . It is this error variance that allows the effect of X_{1ij} to take on different values for different level 2 units. The effect of the second level 1 predictor X_{2ij} , however, does not include a random error variance. Its effect is therefore constrained to be “fixed” or constant across level 2 units. Although measures of explained variance can be calculated for random coefficient and mixed models, these calculations do not account for the additional variance components introduced by the random effects, so it is advisable to perform these calculations on the random intercept only model (see e.g. Snijders and Bosker, 1999: 105).

THE CROSS-LEVEL INTERACTION MODEL

Like ordinary regression models, multilevel models can be further expanded to include interaction terms. These can be incorporated in three basic ways. Individual interactions can be included from cross-product terms for individual level predictors. For instance, victim race and police officer race might be interacted in a study of police use of force (Lawton, 2007). Ecological interactions can also be included using level 2 predictors. Ethnic heterogeneity could be interacted with low socioeconomic

conditions at the neighborhood level, for instance, in a study on risk of victimization (Miethe and McDowall, 1993).¹⁶ Finally cross-level interactions can be included that specify cross-product terms across levels of analysis. For instance, the effects of parental monitoring on problem behavior at the individual level might be expected to vary among neighborhoods with different levels of collective efficacy (Rankin and Quane, 2002). This type of interaction is unique to multilevel analysis so it deserves additional explanation. Equation 11 specifies a cross-level interaction model with 1 individual predictor, 1 ecological predictor and the cross level interaction between them:

$$\begin{array}{ll}
 \text{Level 1} & Y_{ij} = \beta_{0j} + \beta_{1j}X_{1ij} + r_{ij} \\
 \text{Level 2} & \beta_{0j} = \gamma_{00} + \gamma_{01}W_j + u_{0j} \\
 & \beta_{1j} = \gamma_{10} + \gamma_{11}W_j + u_{1j}
 \end{array} \tag{11}$$

This model adds the level 2 predictor W_j to the level 2 equation for β_{1j} , so W_j is now being used to explain variation in the effect of β_{1j} across level 2 units, with the new parameter γ_{11} representing the cross-level interaction between X_{1ij} and W_j . Cross-level interactions are useful for answering questions about *why* individual effects vary across level 2 units; they explicitly model variation in level 1 random coefficients as a product of level 2 group characteristics.¹⁷ Table 9 provides results from a cross-level interaction model examining the conditioning effects of Southern court location on the individual effect of offense severity for federal sentence lengths. The positive interaction effect indicates that offense severity has a stronger effect on sentence length in Southern districts than in does in non-Southern districts. Figure 6 graphs this relationship for values one standard deviation below and above the mean and suggests that although the cross level interaction is statistically significant its substantive magnitude

¹⁶ Depending on the statistical program used, these interactions may or may not be able to be created in the multilevel interface. With HLM, both individual interactions and ecological interactions must be created and all centering adjustments must be made before importing them into the HLM program.

¹⁷ Although conceptually the goal of cross-level interactions is usually to explain significant variation in the effects of level 1 random coefficients across level 2 units, there are instances when theory may dictate examining cross-level interactions for fixed coefficients at level 1 as well. Significant cross-level interactions may emerge involving fixed level 1 coefficients because the significance tests for the cross-level interactions are more powerful than the significance tests produced for random coefficient variance components (Snijders and Bosker, 1999: 74-75).

is fairly modest. As with other multilevel models, cross-level interaction models can easily be extended to the case of multiple predictors at both the individual and group levels of analysis, although care should be taken when including multiple interactions in the same model.

ADDITIONAL CONSIDERATIONS

The preceding examples offer only a rudimentary introduction to the full gamut of multilevel modeling applications but they provide a basic foundation for doing more complex multilevel analysis. The multilevel model can be further adapted to account for additional data complexities that commonly arise in criminological research, including centering conventions, nonlinear dependent variables, and additional levels of analysis. These issues are briefly highlighted below although interested readers should consult comprehensive treatments available elsewhere (e.g. Raudenbush and Bryk, 2002; Luke, 2004; Goldstein, 1995; Snidjers and Bosker, 1999; Kreft and de Leeuw, 1998; Gelman and Hill, 2007).

CENTERING IN MULTILEVEL ANALYSIS

In multilevel models, the centering of variables takes on special importance. Centering, or reparameterization, involves simple linear transformations of the predictor variables by subtracting a constant such as the mean of X or W . Centering in the multilevel framework is no different than in ordinary multiple regression, but it offers important analytical advantages, making model intercepts more interpretable, making main effects more meaningful when interactions are included, reducing collinearity associated with polynomials and interactions, facilitating model convergence in nonlinear models, and simplifying graphical displays of output. Estimates of variance components may also be affected by the centering convention because random coefficients often involve heteroskedastic error variances that depend on the value of X at which they are evaluated (Hox, 2002).

In general, three main centering options are available: no centering, grand-mean centering and group-mean centering. No centering leaves the variable untransformed in its original metric. Although this can be a reasonable approach depending on how the variables are measured, it is usually advisable to employ a centering convention in multilevel analyses for the reasons stated above. The simplest centering convention is grand-mean centering which involves subtracting the overall mean, or the pooled average,

from each observation in the data. The subtracted mean, then, becomes the new zero point so that positive values represent scores above the mean and negative values represent scores below the mean. Grand mean centering is represented as $(X_{ij} - \bar{X}_{..})$ where X_{ij} is the value of X for individual i in group j and $\bar{X}_{..}$ is the grand mean pooled across all observations in the data. Grand mean centering is often useful and rarely detrimental so it offers a good standard centering convention. It only affects the parameter estimates for the model intercept, making the value of the intercept equal to the predicted value of Y when all variables are set to their means. This allows the intercept in a grand-mean centered model to be interpreted as the expected value for the “average” observation in the data.

The alternative to grand mean centering is group mean centering, represented as $(X_{ij} - \bar{X}_{.j})$, where X_{ij} is still the value of X for individual i in group j but $\bar{X}_{.j}$ is now the group-specific mean, so individuals in different level 2 groups have different values of $\bar{X}_{.j}$ subtracted from their scores. Group-mean centering is more complicated than grand-mean centering because it fundamentally alters the meaning and interpretation of both the parameter estimates and the variance components in the multilevel model. It should therefore be used selectively. Luke (2004: 52), for instance, recommended that “one should use group-mean centering only if there are strong theoretical reasons to do so.”¹⁸

In general, centering is always a good idea when a variable has a non-meaningful zero point. For example, it would make little sense to include the UCR crime rate as a predictor variable without first centering it. Otherwise the model intercept would represent the predicted value of Y when the crime rate was equal to 0, which is clearly unrealistic. Even when variables do have meaningful zero points it is often useful to center them. For instance, often times it is even useful to center dummy variables.

Adjusting for the grand mean essentially removes the influence of the dummy variable so that the model intercept represents the expected value of Y for the “average” of that variable rather than for the reference

¹⁸ Some exceptions to this general rule include growth curve modeling with longitudinal data, where the focus is often on separating within and between group regression effects, or research questions involving “frog pond” effects where the theoretical interest is on individual adaptation to one’s specific environment rather than the average effects of individual predictors on the outcome of interest.

category. Similar centering rules apply for ecological variables as for individual level variables, but the important point is that centering decisions should be made *a priori* based on theoretical considerations regarding the desired meaning of model parameters. A number of more detailed treatments offer further detail on the merits and demerits of grand-mean and group-mean centering conventions for multilevel analysis (e.g. Kreft, 1995; Kreft et al. 1995; Longford, 1989; Raudenbush, 1989; Paccagnella, 2006).

GENERALIZED MULTILEVEL MODELS

The examples up to this point all assume a normally distributed continuous dependent variable. Often times, however, criminological research questions involve nonlinear or discrete outcomes, such as binary, count, ordinal or multinomial variables. When this is the case, the multilevel model must be adapted by transforming the dependent variable. For example, dichotomous dependent variables are common in research on crime and justice; whether or not an offender commits a crime, the police make an arrest, or a judge sentences to incarceration all involve binary outcomes (e.g. Eitle et al. 2005; Griffin and Armstrong, 2003; Johnson, 2006). In these cases, the discrete dependent variable often violates assumptions of the general linear model regarding linearity, normality, and homoskedasticity of level 1 errors (Raudenbush and Bryk, 2002). Moreover, because the outcome is bound by 0 and 1, the fitted linear model is likely to produce nonsensical and out of range predictions.

None of these issues are unique to multilevel analysis and the same adjustments used in ordinary regression can be applied to the multilevel model, although some important new issues arise in the multilevel context. Collectively these types of models are labeled generalized hierarchical linear models (GHLM) or just generalized multilevel models, because they provide flexible generalizations of the ordinary linear model. The basic structure of the multilevel model remains the same but the sampling distribution changes. For illustrative purposes, the case of multilevel logistic regression with a dichotomous outcome is illustrated. Equation 12 provides the formula for the unconditional two-level multinomial model using the binomial sampling distribution and the logit link function:¹⁹

¹⁹ The “link function” can be thought of as a mathematical transformation that allows the non-normal dependent variable to be linearly predicted by the explanatory variables in the model.

$$\begin{aligned}
\text{Logit Link Function} \quad \eta_{ij} &= \ln\left(\frac{p}{1-p}\right) \\
\text{Level 1} \quad \eta_{ij} &= \beta_{0j} \\
\text{Level 2} \quad \beta_{0j} &= \gamma_{00} + u_{0j}
\end{aligned} \tag{12}$$

In this formulation, p is the probability of the event occurring and $(1-p)$ is the probability of the event not occurring. p over $(1-p)$, then, represents the *odds* of the event and taking the natural log provides the *log odds*. The dependent variable for the dichotomous outcome is therefore the log of the odds of success for individual i in group j , represented by η_{ij} . The multinomial logistic model is probabilistic, capturing the likelihood that the outcome occurs. Whereas the original binary outcome was constrained to be 0 or 1, p is allowed to vary in the interval 0 to 1, and η_{ij} can take on any real value. In this way, the logistic link function transforms the discrete outcome into a continuous range of values. The level 2 model is identical to that for the continuous outcome presented in Equation 4, but γ_{00} now represents the average log odds of the event occurring across all level 2 units. Equation 13 provides the random coefficient extension of the multilevel logistic model with one random level 1 coefficient and one level 2 predictor:

$$\begin{aligned}
\text{Level 1} \quad \eta_{ij} &= \beta_{0j} + \beta_{1j}X_{1ij} \\
\text{Level 2} \quad \beta_{0j} &= \gamma_{00} + \gamma_{01}W_j + u_{0j} \\
&\quad \beta_{1j} = \gamma_{10} + u_{1j}
\end{aligned} \tag{13}$$

where η_{ij} still represents the log of the odds of success and all the other parameters are the same as previously described.

Notice that in both equations 12 and 13 there is no level 1 variance component included in the multilevel logistic model. This is because the level 1 variance is heteroskedastic and completely determined by the value of p , it is therefore unidentified and not included in the model. This means that the standard formulas for the intraclass correlation and explained variance at level 1 cannot be directly applied to the case of a binary dependent variable.²⁰ Also, most software packages do not provide

²⁰ The level 1 variance in the case of a logistic model is equal to $p(1-p)$ where p is the predicted probability for the level 1 model. The level 1 variance therefore varies as a direct product of the value of p at which the model is

deviance statistics for nonlinear multilevel models. This is because generalized linear models typically rely on “penalized quasi likelihood” (PQL), rather than full or restricted maximum likelihood. This involves a double-iterative process that provides only a rough approximation to the likelihood function on which the deviance is based. In most cases, this means that other methods, such as theory, significance tests for variance components, and robust standard error comparisons must be relied on to properly specify random coefficients in level 1 of the multilevel logistic model.²¹

A third complication involving multilevel models with nonlinear link functions is that two sets of results are produced, one labeled “unit-specific” results and one labeled “population-average” results. Unit-specific results are estimated holding constant the random effects in the model, whereas population-average results are averaged across all level 2 random effects (see Raudenbush and Bryk, 2002: 301). This means that unit-specific estimates model the dependent variable conditional on the random effects in the model, which provides estimates of how the level 1 and level 2 variables affect outcomes *within* level 2 units. Population-average estimates, on the hand, provide the marginal expectation of the outcome averaged across the entire population of level 2 units. If you wanted to know how much an after-school program reduces delinquency for one student compared to another in the same school, then the unit-specific estimate would be appropriate. If you wanted to summarize the average effect of the after-school program on delinquency across all schools, then the population-average estimate would be preferred. In short, which results to report depends on the research question at hand.²² For example, work on racial

evaluated. Although multilevel logistic models do not include a level 1 variance term, some alternative approaches are available for estimating intraclass correlations. For example, Snijders and Bosker, (1999: Chapter 14) discuss reconceptualizing the level 1 model as a latent variable $Z_{ij} = \eta_{ij} + r_{ij}$ in which the level 1 error term is assumed to have a standard logistic distribution with a mean of 0 and variance of $\pi^2/3$. In that case, the intraclass correlation can be calculated as $\rho = \tau_{00}/(\tau_{00} + \pi^2/3)$. This formulation requires the use of the logit link function and relies on the assumption that the level 1 variance follows the logistic distribution. Alternative formulations have also been discussed for the probit link function using the normal distribution (see e.g. Gelman and Hill, 2007: 118).

²¹ PQL estimates are usually sufficient, but tests for random effects based on the PQL likelihood function in models with discrete outcomes may be unreliable, especially for small samples. Alternative full maximum estimators, such as Laplace estimation, are available in some software packages and can be used to test for random effects using the deviance, but this can be computationally intensive.

²² These estimates are often similar but their differences will widen as between-group variance increases and the probability of the outcome becomes farther away from .50 (Raudenbush and Bryk, 2002: 302). In the case of continuous dependent variables the unit-specific and population estimates are identical so this distinction only arises in the case of nonlinear dependent variables.

disparity in sentencing typically reports unit-specific estimates because the focus is on the effect of an offender's race relative to other offenders sentenced in the same court (e.g. Ulmer and Johnson, 2004). Recent work integrating routine activities and social disorganization theory, on the other hand, reports population average estimates because in their words of the authors "our research questions concern aggregate rates of delinquency and unstructured socializing" among all schools (Osgood and Anderson, 2004: 534).

Table 10 reports the unit-specific results with robust standard errors for a random coefficient model examining the likelihood of imprisonment in federal court. The level 1 predictor is the severity of the offense and the level 2 predictor is Southern location. Offense severity exerts a strong positive effect on the probability of incarceration. The coefficient of .26 represents the change in the log odds of imprisonment for a one-unit increase in severity. To make this more interpretable, it is useful to transform the raw coefficient into an odds ratio. Because the left-hand side of Equation 13 represents the log of the odds, we obtain the odds by taking the antilog, in this case $e^{.256} = 1.29$. For each unit increase in the severity of the crime committed, the odds of incarceration increases by a factor of .29 or 29%.²³ The coefficient for South in this model is not statistically significant, suggesting there is no statistical evidence that offenders are more likely to be incarcerated in Southern districts. Turning to the random effects, the level 2 intercept indicates that significant inter-district variation in incarceration remains after controlling for severity and Southern location, and that significant variance exists in the effect of offense severity across districts. Adding the standard deviation to the fixed effect for severity provides a range of coefficients between .20 and .32. Transformed into odds ratios, this means that the effect of offense severity varies between 1.22 and 1.38, so offense severity increases the odds of incarceration between 22% and 38% across one standard deviation (i.e. about two-thirds) of federal districts.

²³ The individual probability of incarceration for individual i in court j can be calculated directly using the formula:

$$P_{ij} = \frac{e^{\gamma_{00} + \gamma_{01}W_j + \gamma_{10}X_{ij}}}{(1 + e^{\gamma_{00} + \gamma_{01}W_j + \gamma_{10}X_{ij}})}, \text{ so with grand-mean centering the mean probability of incarceration is } \bar{P}_{ij} = \frac{e^{\gamma_{00}}}{(1 + e^{\gamma_{00}})}.$$

As with linear multilevel models, generalized multilevel models can be easily extended to the case of multiple predictors at both levels of analysis. In general, similar transformations can be applied for multilevel Poisson, binomial, ordinal and multinomial models by simply applying different link functions to different sampling distributions (see e.g. Raudenbush and Bryk, 2002: Chapter 10; Luke, 2004: 53-62).²⁴ In this way, the basic linear multilevel model can be easily generalized to address a variety of criminological research questions involving different types of discrete dependent variables.

THREE-LEVEL MULTILEVEL MODELS

The basic two-level multilevel linear and generalized models can also be extended to incorporate more complicated data structures that span three or more levels of analysis.²⁵ The basic logic of the multilevel model is the same, but additional error variances are added for each additional level of analysis. The three-level unconditional model for a linear dependent variable is presented in Equation 14:

$$\begin{array}{ll}
 \text{Level 1} & Y_{ijk} = \pi_{0jk} + e_{ijk} \\
 \text{Level 2} & \pi_{0jk} = \beta_{00k} + r_{0jk} \\
 \text{Level 3} & \beta_{00k} = \gamma_{000} + u_{00k}
 \end{array} \tag{14}$$

The *i* subscript indexes level 1 (e.g. students), the *j* subscript indexes level 2 (e.g. classrooms) and the *k* subscript indexes level 3 (e.g. schools). Now level 1 coefficients are represented with π 's, level 2 coefficients with β 's and level 3 coefficients with γ 's, but the three-level structure is purely notational convenience, so it can be simplified through substitution to produce the equivalent but simpler combined model in Equation 15:

$$Y_{ijk} = \gamma_{000} + e_{ijk} + r_{0jk} + u_{00k} \tag{15}$$

Equation 14 and 15 are substantively identical and it becomes clear in the combined model that the outcome Y_{ijk} is modeled as a simple product of an overall intercept γ_{000} plus three different error terms, one for each level of analysis. As in the case of the two-level unconditional model, the three-level model

²⁴ Some important differences emerge in these other contexts, for example, overdispersion frequently occurs in Poisson models for count data, so it is common to incorporate an additional overdispersion parameter in the level 1 model for this type of generalized linear model (see Raudenbush and Bryk, 2002: 295; Gelman and Hill, 2007: 114).

²⁵ Some software packages like HLM are currently limited to three levels of analysis, but other programs (e.g. WLwiN) can analyze up to 10 separate levels of analysis.

parcels the variation in the outcome across levels of analysis. Similar estimates can therefore be calculated for intraclass correlation coefficients, but in the case of the three-level model, there are separate ρ coefficients for level 2 and level 3 of the analysis.²⁶

In the federal court system, cases are nested within district courts but district courts are also nested within circuit courts, which serve as courts of appeal and play an important role in establishing federal case law. Table 10 provides the results from a three-level unconditional model examining federal sentence lengths for the same random sample of 25,000 cases, nested within 89 federal districts, and within 11 federal circuits. The level 2 and level 3 variance components are highly significant, indicating that federal sentences vary significantly across both district and circuit courts. The intraclass correlation coefficients suggest that about 3.5% of the total variation sentencing is between federal districts with another 1.7% between circuit courts. Notice that some of the between-district court variation from the two-level model in Table 3 is now being accounted for by level 3 of the analysis.

As with the two-level model, predictors can be added at each level of analysis. That is, individual predictors can be added at level 1, district court predictors can be added at level 2, and circuit court predictors can be added at level 3. Similar steps can then be taken to identify random coefficients as with the two-level model, but care should be exercised in this process because error structures for three-level models can quickly become complicated. This is because Level 1 variables can be specified as random coefficients at *both* level 2 *and* level 3 of the analysis. Moreover, Level 2 coefficients can also be specified as random effect at level 3 of the analysis. Cross level interactions can occur between levels 1 and 2, levels 1 and 3, or levels 2 and 3. The various possible model specifications can quickly become unwieldy so it is particularly important in three-level models to exercise care in first identifying the hypothesized effects of interest and then properly specifying the model to capture them.

²⁶ The formula for the level 2 intraclass correlation is $\rho_{Level2} = \tau_{\pi} / (\sigma^2 + \tau_{\pi} + \tau_{\beta})$ where σ^2 is the level 1 variance, τ_{π} is the level 2 variance, and τ_{β} is the level 3 variance. The formula for the level 3 intraclass correlation is $\rho_{Level3} = \tau_{\beta} / (\sigma^2 + \tau_{\pi} + \tau_{\beta})$ (see Raudenbush and Bryk, 2002: 230).

Equation 16 provides an example of a basic three-level mixed model with one level 1 predictor, Z_{ijk} , specified as randomly varying across both level 2 and level 3, one level 2 predictor, X_{jk} , fixed at level 3, and no level 3 predictors:

$$\begin{aligned}
 \text{Level 1} \quad & Y_{ijk} = \pi_{0jk} + \pi_{1jk}Z_{ijk} + e_{ijk} \\
 \text{Level 2} \quad & \pi_{0jk} = \beta_{00k} + \beta_{01k}X_{jk} + r_{0jk} \\
 & \pi_{1jk} = \beta_{10k} + r_{1jk} \\
 \text{Level 3} \quad & \beta_{00k} = \gamma_{000} + u_{00k} \\
 & \beta_{01k} = \gamma_{010} \\
 & \beta_{10k} = \gamma_{100} + u_{10k}
 \end{aligned} \tag{16}$$

The subscripts and multiple levels can easily become confusing so it is often useful to examine the combined model substituting levels 2 and 3 into the level 1 equation. Equation 17 provides this reformulation with the fixed effects, or regression coefficients, isolated with parentheses and the random effects, or error variances, isolated with brackets:

$$Y_{ijk} = (\gamma_{000} + \gamma_{100}Z_{ijk} + \gamma_{010}X_{jk}) + [e_{ijk} + r_{0jk} + u_{00k} + r_{1jk}Z_{ijk} + u_{10k}Z_{ijk}] \tag{17}$$

γ_{000} is the overall model intercept, and γ_{100} and γ_{010} are the regression effects for the level 1 and level 2 predictors respectively. As in the unconditional model, e_{ijk} , r_{0jk} and u_{00k} are the level 1, 2 and 3 error variances, and the new error terms $r_{1jk}Z_{ijk}$ and $u_{10k}Z_{ijk}$ indicate that the effect of the level 1 variable, Z_{ijk} , is allowed to vary across both level 2 and level 3 units.

Estimating this model with data on federal sentence lengths produces the output in Table 11. These results report model-based rather than robust standard errors because the highest level of analysis includes only 11 circuit courts. The effect of offense severity is essentially the same, increasing sentence length by about 5.7 months, but the effect for Southern location has been attenuated and is now only marginally significant. This likely reflects the fact that some of the district variation is now being accounted for by the circuit level of analysis. The random effects in Table 11 support this interpretation. The level 2 variance component is smaller than it was in the two-level model reported in Table 8. Notice also that there are two variance components associated with offense severity because its effect is allowed

to vary both across district and circuit courts. The magnitude of these variance components indicates there is more between-district than between-circuit variation in the effect of offense severity, but both are highly significant. Although conceptually the three-level multilevel model represents a straightforward extension of the two-level model, in practice care needs to be exercised to avoid exploding complexity (for recent examples using 3 level models see Duncan et al., 2003; Johnson, 2006; Wright et al. 2007).

SUMMARY AND CONCLUSIONS

Multilevel models represent an increasingly popular analytical approach in the field of criminology. According to a recent analysis by Gary Kleck (2006), between 5% and 6% of empirical research papers in top criminology journals utilize multilevel modeling techniques; interestingly, though, 14% of these were published in the flagship journal for the field, *Criminology*. Given the omnipresence of multilevel research questions in criminology, the use of multilevel analysis will continue to gain prominence in the field. Because multilevel models provide a sophisticated approach for integrating multiple levels of analysis, they represent an important opportunity to expand theoretical and empirical discourse across a variety of criminological domains. Multilevel models have already been used to study a rich diversity of topics, from examinations of self-control (Hay and Forrest, 2006; Doherty, 2006; Wright and Beaver, 2005) and strain theory (Slocum et al. 2005) to life course perspectives (Horney et al. 1995; Sampson et al. 2006) and analyses of violent specialization (Osgood and Schreck, 2007) – from crime victimization (Xie and McDowall, 2008; Wilcox et al. 2007), policing (Rosenfeld et al. 2007; Warner, 2007) and punishment outcomes (Kleck et al. 2005; Bontrager et al. 2005; Johnson, 2005; 2006) to post-release recidivism (Kubrin and Stewart, 2005; Chiricos et al. 2007; Mears et al. 2008) and program evaluations (Gottfredson et al. 2007; Esbensen et al. 2001) – across a broad range of criminological topic areas, multilevel models have proven to be invaluable tools.

Despite their many applications, though, the old adage that “A little bit of knowledge can be a dangerous thing” applies directly to multilevel modeling. Modern software packages make estimating multilevel models relatively simple, but the fully specified multilevel model often contains complicated error structures that can easily be misspecified. Moreover, these complexities can sometimes result in

instability in parameter estimates. This is particularly the case for ecological predictors and for three-level and generalized linear models. For instance, it is common for ecological predictors to have shared variance (Land et al. 1990), so inclusion or elimination of one predictor can often affect the estimates for other predictors in the model. It is therefore essential that the final model be carefully constructed from the ground up, performing model diagnostics to test for misspecification, investigating problematic collinearity and examining alternative models to ensure that the final estimates are robust to minor alterations in model specification.

Although this chapter provides a basic overview of multilevel models, it is important to note that it does not cover many of their advanced applications such as longitudinal data analysis, growth-curve modeling, time series data, latent variable analysis, meta-analytical techniques or analysis of cross-classified data. Beyond situations where individuals are influenced by social contexts, multilevel data commonly characterizes these and many other criminological enterprises. As a discipline, we are just beginning to incorporate the full range of applications for multilevel statistical models in the study of crime and punishment. The goals of this chapter were simply to introduce the reader to the basic multilevel model, to emphasize the ways in which it is similar to and different from the ordinary regression model, to provide some brief examples of different types of multilevel models and to demonstrate how they can be estimated within the context of jurisdictional variations in federal criminal punishments across court contexts.

Figure 1: The Hierarchical Nature of Multiple Units of Analysis in Multilevel Models

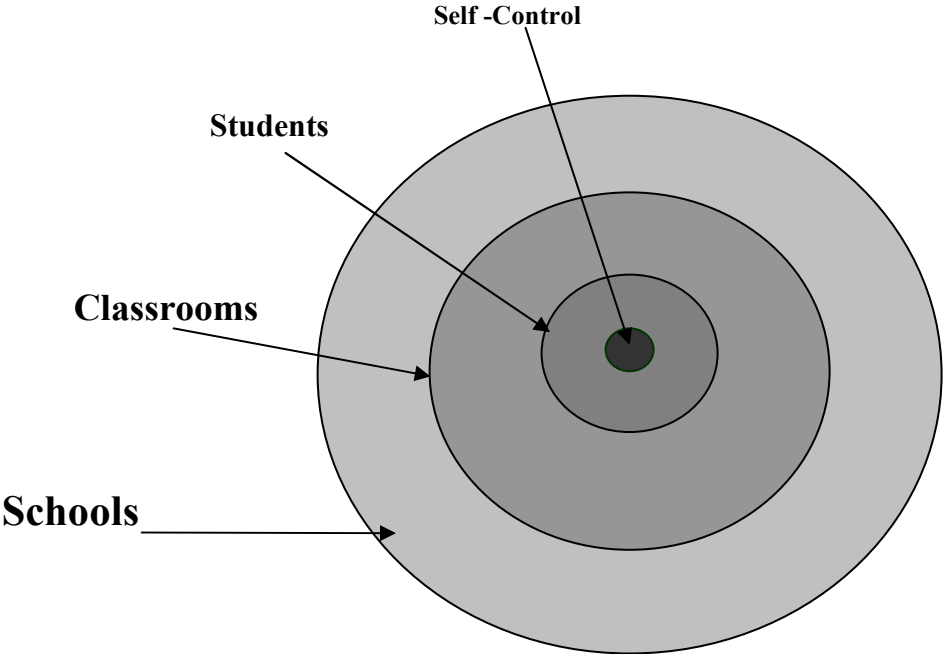


Figure 2: The Nesting of Multilevel Data across Levels of Analysis

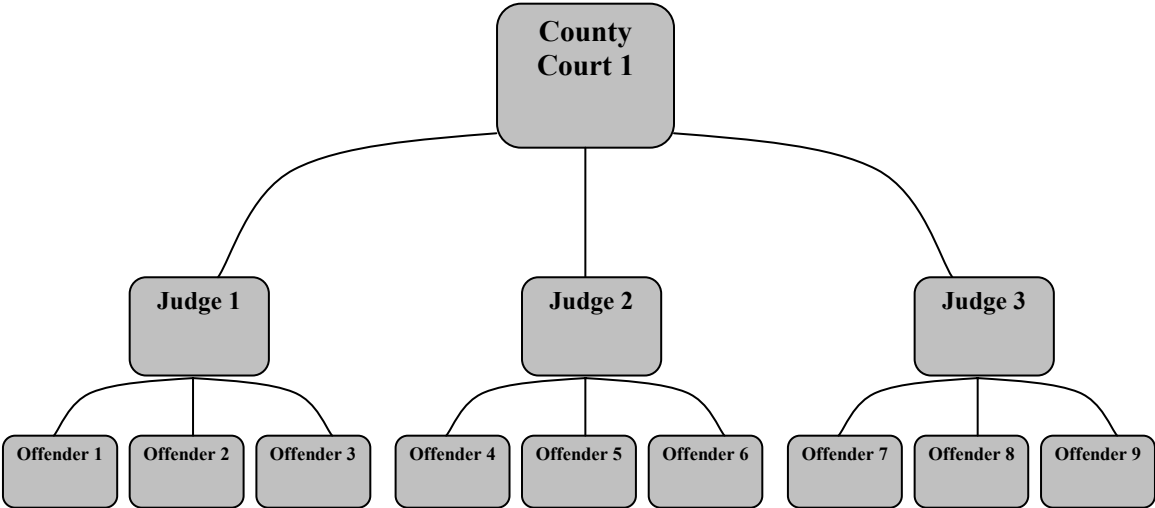


Figure 3: Variation in Trial Penalties across Federal Courts

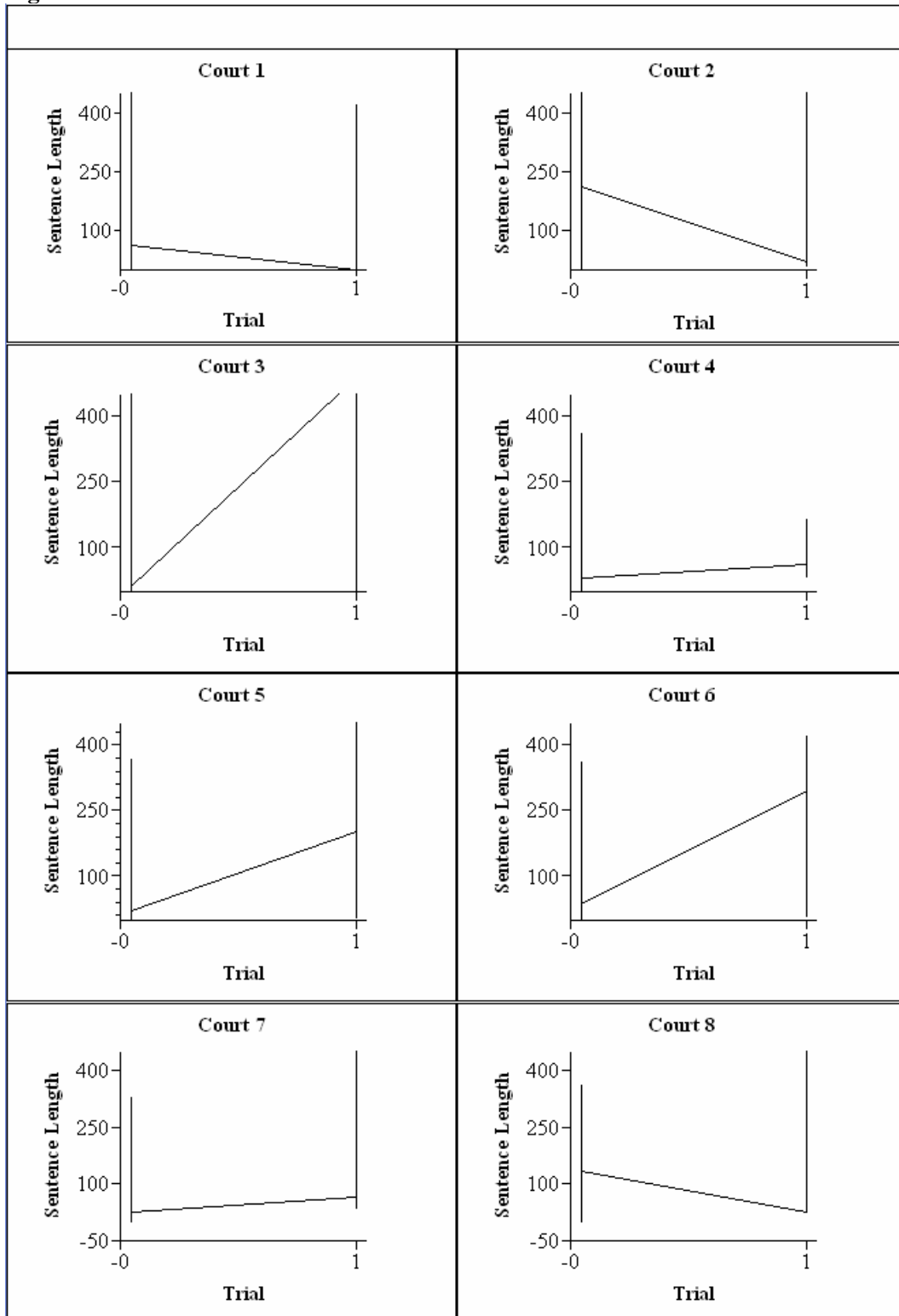
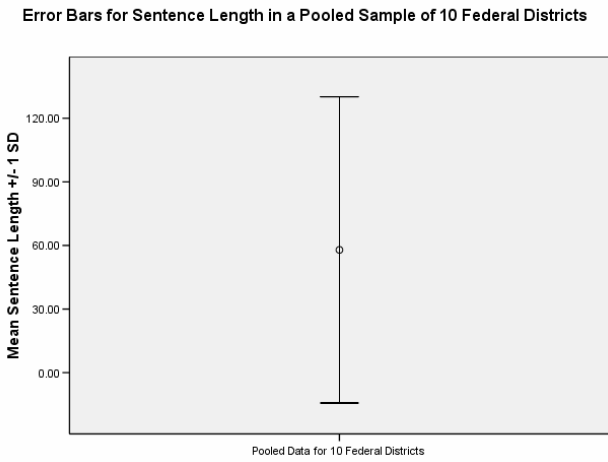


Figure 4: Variation in Sentence Lengths across Federal Courts

Panel A: Pooled Data for Sample of 10 Districts



Panel B: Disaggregated Data for Sample of 10 Districts

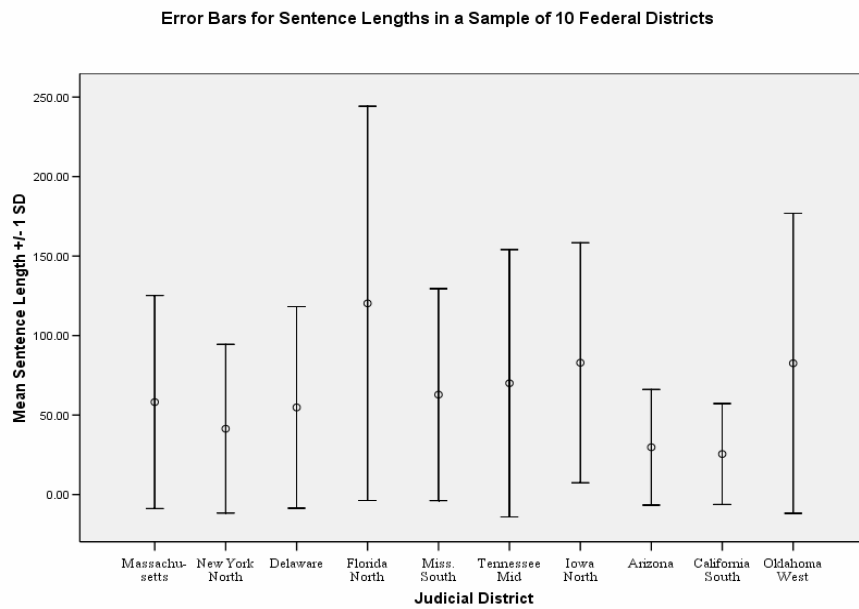


Figure 5: Comparison of Random Intercept and Random Coefficient Models

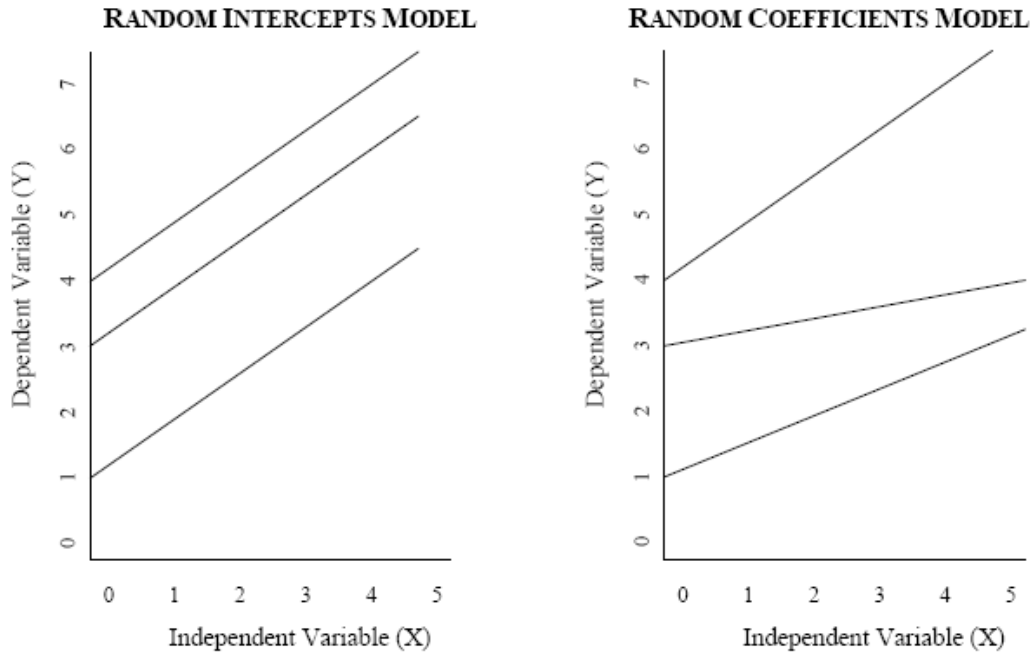


Figure 6: Cross Level Interaction of Offense Severity and Southern Location

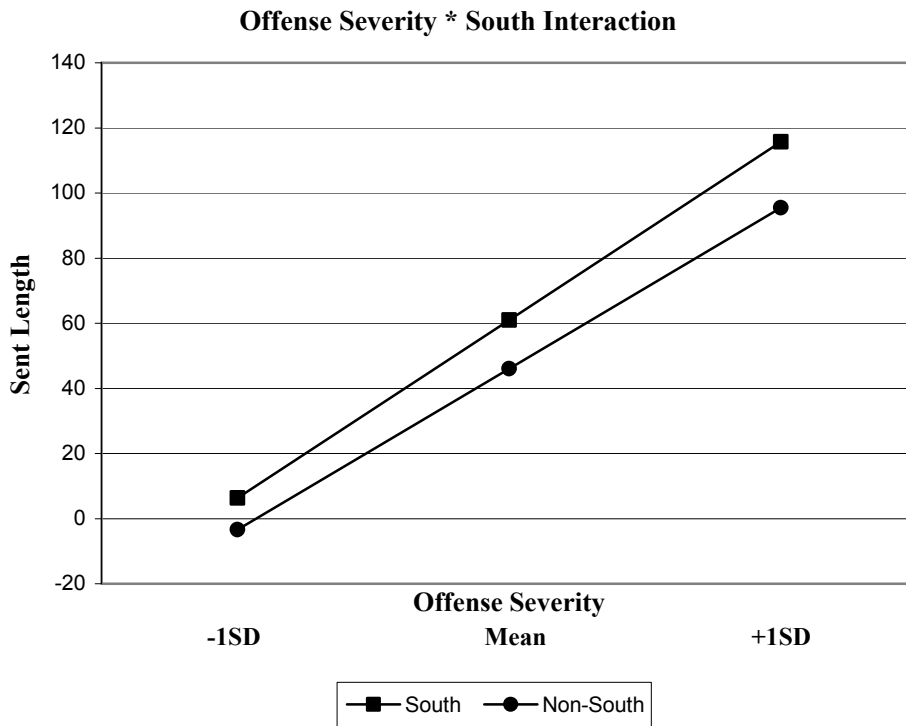


Table 1: Recent Examples of Multilevel Studies Published in *Criminology* from 2005 to 2008

Author(s)	Year	Topic
Xie and McDowall	2008	Victimization and Residential Mobility
Schreck, Stewart, and Osgood	2008	Violent Offender and Victim Overlap
Johnson, Ulmer and Kramer	2008	Federal Guidelines Departures
Xie and McDowall	2008	Residential Turnover and Victimization
Mears, Wang, Hay and Bales	2008	Social Context and Recidivism
Zhang, Messner and Liu	2007	Crime Reporting in China
Kreager	2007	School Violence and Peer Acceptance
Wilcox, Madensen and Tillyer	2007	Guardianship and Burglary Victimization
Chiricos, Barrick, Bales, and Bontrager	2007	Labeling and Felony Recidivism
Osgood and Shreck	2007	Stability and Specialization in Violence
Rosenfeld, Fornango, and Rengifo	2007	Order-Maintenance Policing and Crime
Bernburg and Thorlindsson	2007	Community Structure and Delinquency
Warner	2007	Social Context and Calls to Police
Hay and Forrest	2006	The Stability of Self-Control
Doherty	2006	Self-Control, Social Bonds, and Desistence
Griffin and Wooldredge	2006	Sex Disparities in Imprisonment
Sampson, Laub, and Wimer	2006	Marriage and Crime Reduction
Ulmer and Bradley	2006	Trial Penalties
Johnson	2006	Judge and Court Context in Sentencing
Kubrin and Stewart	2006	Neighborhood Context and Recidivism
Simons, Simons, Burt, Brody, and Cutrona	2005	Collective Efficacy, Parenting and Delinquency
Slocum, Simpson, and Smith	2005	Strain and Offending
Wright and Beaver	2005	Parental Influence and Self-Control
Bontrager, Bales, and Chiricos	2005	Race and Adjudicated Guilt
Kleck, Sever, Li, and Gertz	2005	Perceptions of Punishment
Johnson	2005	Sentencing Guidelines Departures

Table 2: Glossary of Multilevel Modeling Terminology

Terminology	Definition
Aggregate Variable	Ecological variable created by aggregating the individual properties of lower level measures up to the group level of analysis. Also sometimes referred to as "Derived" or "Analytical" variables.
Atomistic Fallacy	The fallacy, also referred to as the Individualistic Fallacy, that results when faulty inferences for macro level group relationships are drawn using micro-level individual data. See Ecological Fallacy
Compositional Effects	Between group differences in outcomes that are attributable to differences in group composition, or in the different individuals of which the groups are comprised.
Contextual Analysis	Early analytical approach designed to investigate the effects of aggregate characteristics of the collective by including aggregate variables along with individual variables in traditional regression models.
Contextual Effects	Macro-level influences exerted by aggregate variables above and beyond those attributable to compositional differences in groups, but sometimes the term is used to refer to any group level effects.
Contextual Effects Model	Statistical model that include individual characteristics and the aggregates of the individual characteristics in the same model in order to assess the influence of contextual effects on individual outcomes.
Cross-Level Interaction	A statistical interaction between higher and lower order variables, usually attempting to explain variation in the effects of lower level measures across higher level groupings.
Cross Classified Model	A multilevel statistical model for analyzing data that is cross-nested in two or more higher levels of analysis which are not strictly hierarchical in structure. Also referred to as cross-nested models.
Ecological Fallacy	The fallacy that results when faulty inferences for individual level relationships are made using group level data. (see Atomistic Fallacy)
Ecological Variable	A broad term for any higher order group level variable, including aggregate, structural and global measures. Sometimes referred to as a Group Level, Macro Level, or Level 2 variables.
Empirical Bayes Estimates	Estimates for group level parameters that are optimally weighted to combine information from the individual group itself with information from other similar groups in the data. See Conditional Shrinkage.
Fixed Effects	Regression coefficients (or intercepts) that are not allowed to vary randomly across higher level units. These are sometimes referred to as fixed coefficients. See Random Effects/Coefficients.
Fixed Effects Models	Statistical models in which all all effects or coefficients are fixed. Often this refers to the case where a dummy variable is included for each higher level unit to remove between-group variation in the outcome.

Global Variable	A group level variable that unlike Aggregate Variables has no individual analogue. Global (or Integral) Variables refer to characteristics that are uniquely defined at the higher level of analysis.
Group Level Variable	An alternative name for ecological variables that measure any group level characteristic. Sometimes referred to as Level 2 Variables. See Individual Variable.
Hierarchical (Linear) Model	A multilevel model for analyzing data that is nested among two or more hierarchies. Hierarchical models technically assume that data are strictly nested across levels of analysis, although this term may refer to multilevel models generally.
Individual Level Variable	A variable that characterizes individual attributes or refers to individual level constructs. Sometimes referred to as Level 1 Variables. See Group Level Variable.
Intraclass Correlation	The proportion of the total variance in the outcome that exists between groups or higher level units rather than within groups or higher level units.
Mixed Model	A multilevel model containing both fixed and random coefficients. Some regression coefficients are allowed to vary randomly across higher level units while other regression coefficients are specified as fixed coefficients.
Multilevel Analysis	An analytical approach for simultaneously analyzing both individual and group level effects when data is measured at two or more levels of analysis with lower level (micro) observations nested within higher level (macro) units.
Multilevel Model	A statistical model used in multilevel analysis for analyzing data that is measured at two or more levels of analysis, including but not limited to hierarchical linear models, hierarchical nonlinear models, and cross-classified models.
Population Average Estimates	Estimates for nonlinear multilevel models that provide the marginal expectation of the outcome averaged across all random effects rather than after controlling for random effects. See Unit-Specific Estimates
Random Coefficient Model	A multilevel statistical model in which the individual level intercept and regression coefficients are allowed to have randomly varying effects across higher level units of analysis. See Random Intercept Model.
Random Effects	Regression coefficients (or intercepts) that are allowed to vary randomly across higher level units. These are sometimes referred to as random intercepts or random coefficients. See Fixed Effects.
Random Intercept Model	A multilevel statistical model in which the individual level intercept is allowed to vary randomly across higher level units of analysis, but the individual level coefficients are assumed to have constant effects. See Random Coefficient Model.
Unit Specific Estimates	Estimates for nonlinear multilevel models that are conditional on higher level random effects. Unit specific models provide individual estimates controlling for rather than averaging across random effects. See Population Average Estimates
Variance Components	Model parameters (sometimes referred to as random effects) that explicitly capture both within-group and between-group variability in outcomes. Each level of analysis in a multilevel model has its own variance component.

Table 3: Unconditional HLM Model of Federal Sentence Lengths

Sentence Length in Months						
<u>Fixed Effects</u>		<u>b</u>	<u>S.E.</u>	<u>df</u>	<u>p-value</u>	
	Intercept (γ_{00})	52.5	1.8	88	0.00	
<u>Random Effects</u>		<u>s²</u>	<u>S.D.</u>	<u>df</u>	<u>p-value</u>	<u>ρ</u>
	Level 1 (r_{ij})	4630.0	68.0			
	Level 2 (u_{oj})	267.1	16.3	88	0.00	0.055
Deviance = 282173.7						
Parameters = 2						
N=25,000						

Table 4: Random Intercept Model of Federal Sentence Lengths

Sentence Length in Months						
<u>Fixed Effects</u>		<u>b</u>	<u>S.E.</u>	<u>df</u>	<u>p-value</u>	
	Intercept (γ_{00})	51.0	1.1	88	0.00	
	Severity (β_1)	5.6	0.2	24998	0.00	
<u>Random Effects</u>		<u>s²</u>	<u>S.D.</u>	<u>df</u>	<u>p-value</u>	
	Level 1 (r_{ij})	2228.7	47.2			
	Level 2 (u_{oj})	93.2	9.7	88	0.00	
Deviance = 263875.9						
Parameters = 2						
N=25,000						

Table 5: Random Intercept Model of Federal Sentence Length

Sentence Length in Months

<u>Fixed Effects</u>	<u>b</u>	<u>S.E.</u>	<u>df</u>	<u>p-value</u>
Intercept (γ_{00})	50.9	1.0	87	0.00
South (γ_{01})	7.1	2.3	87	0.00
Severity (β_1)	5.6	0.2	24997	0.00
<u>Random Effects</u>	<u>s²</u>	<u>S.D.</u>	<u>df</u>	<u>p-value</u>
Level 1 (r_{ij})	2228.7	47.2		
Level 2 (u_{oj})	82.4	9.1	87	0.00

Deviance = 263860.9

Parameters = 2

N=25,000

Table 6: Random Coefficient Model of Federal Sentence Length

Sentence Length in Months

<u>Fixed Effects</u>	<u>b</u>	<u>S.E.</u>	<u>df</u>	<u>p-value</u>
Intercept (γ_{00})	49.7	1.0	88	0.00
Severity (β_1)	5.7	0.1	88	0.00
<u>Random Effects</u>	<u>s²</u>	<u>S.D.</u>	<u>df</u>	<u>p-value</u>
Level 1 (r_{ij})	2098.7	45.8		
Level 2 (u_{oj})	78.7	8.9	88	0.00
Severity (u_{lj})	1.4	1.2	88	0.00

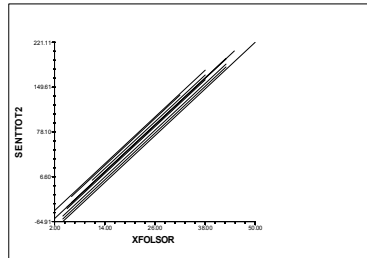
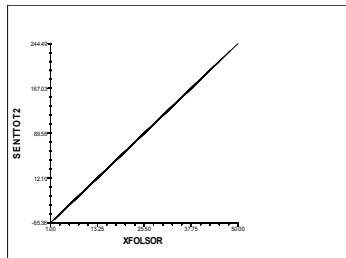
Deviance = 262530.1

Parameters = 4

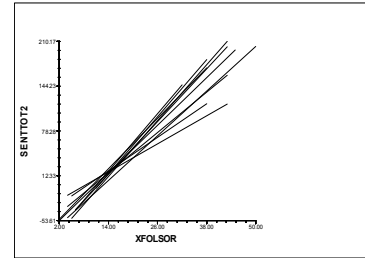
N=25,000

Table 7: Comparison of OLS, Random Intercept and Random Coefficient Models

OLS REGRESSION			RANDOM INTERCEPT			RANDOM COEFFICIENT		
<i>Without Robust Errors</i>			<i>Without Robust Errors</i>			<i>Without Robust Errors</i>		
	b	S.E.		b	S.E.		b	S.E.
Intercept	47.9	0.30	Intercept	51.0	1.10	Intercept	49.7	1.02
Offense Severity	5.6	0.03	Offense Severity	5.6	.03	Offense Severity	5.7	.13
<i>With Robust Errors</i>			<i>With Robust Errors</i>			<i>With Robust Errors</i>		
	b	S.E.		b	S.E.		b	S.E.
Intercept	47.9	0.30	Intercept	51.0	1.06	Intercept	49.7	1.01
Offense Severity	5.6	0.03	Offense Severity	5.6	.19	Offense Severity	5.7	.13



Deviance = 263875.9
Parameters = 2



Deviance = 262530.1
Parameters = 4

Table 8: Random Coefficient Model with Level 2 Predictor of Federal Sentence Length
Sentence Length in Months

<u>Fixed Effects</u>	<u>b</u>	<u>S.E.</u>	<u>df</u>	<u>p-value</u>
Intercept (γ_{00})	49.6	1.0	87	0.00
South (γ_{01})	3.4	1.4	87	0.02
Severity (β_1)	5.7	0.1	88	0.00
<u>Random Effects</u>	<u>s²</u>	<u>S.D.</u>	<u>df</u>	<u>p-value</u>
Level 1 (r_{ij})	2098.6	45.8		
Level 2 (u_{oj})	71.6	8.5	87	0.00
Severity (u_{lj})	1.5	1.2	88	0.00

Table 9: Cross-Level Interaction Model of Federal Sentence Length

Sentence Length in Months

<u>Fixed Effects</u>	<u>b</u>	<u>S.E.</u>	<u>df</u>	<u>T-ratio</u>	<u>p-value</u>
Intercept (γ_{00})	49.6	1.0	87	49.14	0.00
South (γ_{01})	6.3	2.0	87	3.37	0.02
Severity (β_1)	5.7	0.1	88	42.45	0.00
South*Severity (γ_{11})	0.6	0.3	87	2.07	0.04

<u>Random Effects</u>	<u>s²</u>	<u>S.D.</u>	<u>df</u>	<u>χ^2</u>	<u>p-value</u>
Level 1 (r_{ij})	2098.6	45.8			
Level 2 (u_{oj})	70.2	8.4	87	1130.14	0.00
Severity (u_{lj})	1.4	1.2	88	1644.40	0.00

Deviance = 262519.3

Parameters = 4

N=25,000

Table 10: Multilevel Logistic Model of Federal Incarceration

Prison vs. No Prison (Unit-Specific Model with Robust Standard Errors)

<u>Fixed Effects</u>	<u>b</u>	<u>S.E.</u>	<u>df</u>	<u>p-value</u>	<u>Odds Ratio</u>
Intercept (γ_{00})	2.80	0.08	87	0.00	
South (γ_{01})	0.07	0.11	87	0.53	1.07
Severity (β_1)	0.26	0.01	88	0.00	1.29

<u>Random Effects</u>	<u>s²</u>	<u>S.D.</u>	<u>df</u>	<u>p-value</u>
Level 2 (u_{oj})	.41	0.64	87	0.00
Severity (u_{lj})	.004	0.06	88	0.00

Table 11: Three-Level Unconditional Model of Federal Sentence Length

Sentence Length in Months

<u>Fixed Effects</u>	<u>b</u>	<u>S.E.</u>	<u>df</u>	<u>p-value</u>	
Intercept (γ_{000})	52.5	3.2	10	0.00	
<u>Random Effects</u>	<u>s²</u>	<u>S.D.</u>	<u>df</u>	<u>p-value</u>	<u>ρ</u>
Level 1 (e_{ijk})	4630.1	68.0			
Level 2 (r_{0jk})	172.5	15.2	78	0.00	0.035
Level 3 (u_{00k})	85.2	9.2	10	0.00	0.017

Table 12: Three-Level Mixed Model of Federal Sentence Length

Sentence Length in Months

<u>Fixed Effects</u>	<u>b</u>	<u>S.E.</u>	<u>df</u>	<u>p-value</u>
Intercept (γ_{000})	48.6	1.6	10	0.00
South (β_{01k})	2.8	1.7	87	0.10
Severity (π_{1jk})	5.7	0.2	10	0.00
<u>Random Effects</u>	<u>s²</u>	<u>S.D.</u>	<u>df</u>	<u>p-value</u>
Level 1 (e_{ijk})	2098.6	45.8		
Level 2 (r_{0jk})	53.6	7.3	77	0.00
Severity (r_{1jk})	1.1	1.1	78	0.00
Level 3 (u_{00k})	17.6	4.2	10	0.00
Severity (u_{10k})	0.3	0.5	10	0.00

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